

$$\mathcal{Z}\{a^k\} = \frac{z}{z-a}$$

$$\mathcal{Z}\{1\} = \frac{z}{z-1}$$

$$\mathcal{Z}\{(-1)^k\} = \frac{z}{z+1}$$

$$\mathcal{Z}\{a\} = \frac{az}{z-1}$$

$$\mathcal{Z}\{k^p\} = -z \frac{d}{dz} \mathcal{Z}\{k^{p-1}\}$$

$$\mathcal{Z}\{k f(k)\} = -z \frac{d}{dz} \mathcal{Z}\{f(k)\}$$

$$\mathcal{Z}\{a^{-k} f(k)\} = \mathcal{Z}\{f(ak)\}$$

$$\mathcal{Z}\{k^p f(k)\} = \left(-z \frac{d}{dz}\right)^p \mathcal{Z}\{f(k)\}$$

$$\mathcal{Z}\{k\} = \frac{z}{(z-1)^2}$$

$$\mathcal{Z}\{k^2\} = \frac{z^2 + z}{(z-1)^3}$$

$$\mathcal{Z}\{a^k \cdot k\} = \frac{az}{(z-a)^2}$$

$$\mathcal{Z}\{a^k k^2\} = \frac{az^2 + a^2 z}{(z-a)^3}$$

$$\mathcal{Z}\{\cos bk\} = \frac{z(z - \cos b)}{z^2 - 2z \cos b + 1}$$

$$\mathcal{Z}\{\sin bk\} = \frac{z \sin b}{z^2 - 2z \cos b + 1}$$